

# Volume of Prisms <sup>Key</sup>

As you recall, volume is the number of cubic units it takes to fill an object. Some examples of how to measure volume are in<sup>3</sup>, cu.cm, ft<sup>3</sup>, cubic yds, and m<sup>3</sup>.

A prism is a 3 - dimensional object with 2 congruent bases that are parallel and polygons and all the rest of the faces are rectangles.

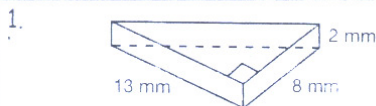
To find the volume of a prism, you could fill the object with \_\_\_\_\_ and then count them very carefully. Another way to find the volume of a prism is to use the formula below:

$$V = Bh$$

**B** → the area of the base

**h** → the distance between the bases  
(or the # of layers)

Find the volume of the two prisms below using the formula above.

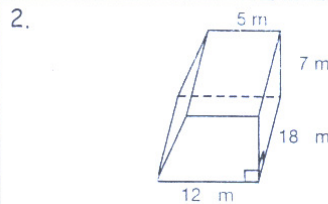


$$V = Bh$$

B = area of triangle  
 $\frac{1}{2}(13)(8)$   
 52

$$V = (52\text{mm}^2)(2\text{mm})$$

$$V = 104\text{mm}^3$$



$$V = Bh$$

B = area of trapezoid  
 $\frac{1}{2}(5+12)7$   
 59.5

$$V = (59.5)18$$

$$V = 1071\text{m}^3$$

As you did in last night's homework, write the formulas for the volume of the given objects.

Rectangular solid...  $V = LWH$       Cube...  $V = e^3$       Cylinder...  $V = \pi r^2 h$

Some questions to consider...

- Is a rectangular solid a prism? yes
- Is a cube a prism? yes
- Is a cylinder a prism? no

Why or why not? ✓  
 Why or why not? ✓  
 Why or why not? not polygonal base

Some ideas to think about...

The rectangular solid and the cube are prisms. Therefore, the formula  $V = Bh$  should work for them as well. How are the formulas really the same?

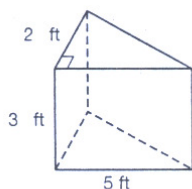
$V = l \cdot w \cdot h \rightarrow$  The  $l \cdot w =$  the area of the rectangular base ( $B$ )

$V = e \cdot e \cdot e \rightarrow$  The  $e \cdot e =$  the area of the square base ( $B$ )

The cylinder is not a prism. However, how is the formula,  $V = \pi r^2$  similar to the formula  $V = Bh$  for the prism?  $\pi r^2$  is the area of a circle; the cylinder has bases that are circles.

Find the volume for the figures below using the formula,  $V = Bh$ .

3.



$$V = Bh$$

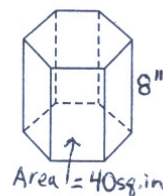
$$V = (5\text{ft}^2)(3)$$

$$V = 15\text{ft}^3$$

$$B = \text{area of triangular base}$$

$$\frac{1}{2} \cdot 2 \cdot 5 = 5$$

4.

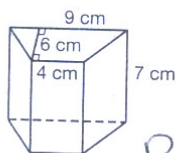


$$V = Bh$$

$$V = 40(8)$$

$$V = 320 \text{ cu. in.}$$

5.



$$V = Bh$$

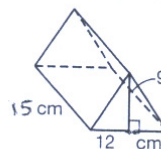
$$V = 39.7$$

$$V = 273 \text{ cm}^3$$

$$B = \text{area of trapezoid}$$

$$\frac{1}{2}(4+9) \cdot 6 = 39$$

6.



$$V = Bh$$

$$V = 54 \cdot 15$$

$$V = 810 \text{ cm}^3$$

$$B = \text{area of a } \Delta$$

$$\frac{1}{2} \cdot 12 \cdot 9 = 54$$